

# In-Processing Fairness Improvement Methods for Regression Data-Driven Building Models: Achieving Uniform Energy Prediction

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## Abstract

In recent years, the massive data collection in buildings has paved the way for the development of accurate data-driven building models (DDBMs) for various applications. However, a model with a high overall accuracy would not ensure a good predictive performance on all conditions. The biased predictive performance for some conditions may cause fairness problems. Although pre-processing methods were proposed to improve predictive fairness by removing discrimination from training datasets for classification problems in building engineering domain, they lack the ability of achieving user-defined trade-off between fairness and accuracy for regression problems, such as energy prediction. To improve the predictive fairness of regression models in terms of having similar predictive performance between different conditions, this study proposes four in-processing methods, namely mean residual difference penalized (MRDP) regression, mean square error penalized (MSEP) regression, mean residual difference constrained (MRDC) regression, and mean square error constrained (MSEC) regression, to add fairness-related penalties or constraints to the loss function of regression models. Then, these proposed methods are applied to develop linear regression models for energy prediction of an apartment. In this case study, improving predictive fairness means to let the energy predictive accuracy be uniform no matter if there is occupancy movement. The result shows that MSEC is the most powerful method to improve fairness in terms of mean square error (MSE) rate and mean absolute error (MAE) rate, while MSEP is another good option to improve fairness without a significant decrease on the overall accuracy. MRDC is effective on improving the similarity of absolute mean residual difference ( $\text{abs}(\text{MRD})$ ) between different conditions, however, MRDP would not affect the predictive result.

**Keywords:** Fairness; Accuracy; Data-driven model; Energy prediction; Building

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## 1 **1. Introduction**

2 In recent years, the widespread installation of smart sensors, Internet-of-Things, and smart  
3 home energy management systems (HEMSs) makes buildings data-rich [1]. The abundant data  
4 could be utilized to train data-driven models to represent building states, such as indoor air  
5 temperature [2], indoor air quality [3], HVAC operation status [4,5], energy consumption [6,7],  
6 etc. Among these models, energy prediction models could be integrated into model predictive  
7 controller to provide optimal control signals for building energy management systems to achieve  
8 energy saving, cost saving, and/or peak shifting [8]. Accurate energy prediction could also benefit  
9 suppliers in energy generation and distribution planning [9].

10 Existing energy prediction models mainly treat energy prediction as regression problems  
11 whose outputs are continuous values [10]. The primary aim of these models is to be accurate  
12 enough so that predictive results are close enough to measured values. Commonly used accuracy  
13 measures for these regression models include MAE, MAPE, RMSE, CV(RMSE),  $R^2$ , etc. [11].  
14 However, a high overall accuracy could not ensure the predictive performance is fairly perfect in  
15 different conditions. In fact, improving predictive performance similarity between distinct  
16 conditions could ensure that the predictive model provides a fair service to the users by ensuring  
17 them to receive a uniform predictive performance. For instance, if one energy predictive model is  
18 more accurate when some occupants are in the building than the period that some other occupants  
19 are in the building, energy scheduling service provided based on the model would be more efficient  
20 for the former occupants, thus, it would be unfair to other ones who receive less accurate  
21 information.

22 Fairness problems are varied and could mainly be classified into three categories based on  
23 the relationship between predictive results and the protected attribute(s) [12]: *Type I*. The predicted  
24 output is independent of the protected attribute(s). *Type II*. The predictive performance is similar  
25 across classes/conditions defined by the protected attribute(s). *Type III*. The predicted output is  
26 independent of the predictive probability score for samples coming from different  
27 classes/conditions defined by the protected attribute(s). Here, protected attributes are also called  
28 sensitive attributes. They define conditions in which the predictive result is not willing to be biased.  
29 For instance, race, age, gender, occupancy-related data (e.g., occupancy status, occupancy count,  
30 and occupants' occupation, etc.) are commonly used protected attributes because different

1 predictive service for conditions defined by them could cause discrimination problems. Note that  
2 achieving different types of fairness at the same time is almost impossible [13] because of their  
3 distinct evaluation criteria. Thus, researchers are recommended to clearly define which type of  
4 fairness that they plan to achieve. In this study, achieving fairness refers to have uniform predictive  
5 accuracy among different conditions defined by the protected attribute (i.e., *Type II* fairness).

6 One probable reason behind the distinct predictive accuracy of different conditions is the  
7 imbalanced training dataset. For instance, in reality, most operation data of HVAC devices are of  
8 normal status, while only a few are in faulty condition. As a result, the data-driven model trained  
9 based on this imbalanced dataset would work perfectly on predicting normal status, but show  
10 worse performance for faulty detection. Therefore, to narrow the predictive performance between  
11 different conditions, one useful way is to reduce the discrimination among training dataset. In other  
12 word, it means to produce a balanced training dataset that contains a similar amount of data for all  
13 conditions. These methods belong to data pre-processing methods.

14 The easiest way to get a balanced training dataset is to oversample for minority conditions  
15 and/or undersample for majority conditions. For instance, the synthetic minority oversampling  
16 technique (SMOTE) that samples data for minority conditions by linear interpolation between  
17 minority samples has been used to oversample faulty samples to increase the fault detection  
18 accuracy of HVAC devices [14,15]. However, large oversampling size may increase the  
19 classification uncertainty because of the change in data distribution. Furthermore, this method has  
20 not been used to solve fairness problems. To eliminate the bias among conditions defined by the  
21 protected attribute and output label, Kamiran and Calders [16] proposed uniform sampling and  
22 preferential sampling: uniform sampling randomly duplicate data for minority conditions or delete  
23 data from majority conditions, while preferential sampling duplicate/delete data that closest to the  
24 decision boundary. However, these methods have not been applied to omit the bias among the  
25 training dataset of data-driven building models (DDBMs). To remove discrimination from the  
26 training dataset of DDBMs, we proposed four types of data pre-processing methods, namely  
27 sequential sampling, sequentially balanced preferential sampling, reversed preferential sampling,  
28 and sequential preferential sampling, to produce a balanced training dataset for classification  
29 problems. The generalizability of these proposed methods on fairness and accuracy of DDBMs is  
30 compared with uniform sampling and preferential sampling in [12,17].

1 Besides, generating representative data is an efficient way to enrich data points in minority  
2 conditions. For instance, Yan et al. [5] applied the generative adversarial network (GAN) to  
3 generate faulty training samples for fault detection and diagnosis (FDD) of air handling units  
4 (AHUs). Their study found that the re-balanced training dataset could improve the diagnostic  
5 accuracy of traditional data-driven models (e.g., random forest (RF), support vector machine  
6 (SVM), multi-layer perceptron (MLP), k-nearest-neighbor (KNN) and decision tree (DT)) from  
7 nearly 50% to almost 100%. Yan et al. [19] have also applied the GAN to re-balance the training  
8 dataset for automatic FDD for chillers. Li et al. [1] proposed a GAN to improve the diagnostic  
9 accuracy for building HVAC systems by taking advantage of the re-balanced labeled and unlabeled  
10 data. However, these data generative models usually face the non-convergence issue [20]. Besides,  
11 the representativity of created data would highly affect the predictive performance, including  
12 fairness and accuracy.

13 These data pre-processing methods could eliminate bias among training dataset, and thus,  
14 improve the predictive accuracy among minority conditions. However, it could not quantitatively  
15 ensure that the predictive accuracy is similar enough between different conditions. Besides, data  
16 pre-processing methods are more suitable for classification problems because conditions defined  
17 by the output label and protected attribute are less and easier to be determined.

18 To quantitatively define the required performance similarity for regression problems like  
19 building energy consumption, in-processing methods that set fairness-related constraints or  
20 penalties in the loss function of model training would be a good option [21]. In-processing methods  
21 could achieve specific fairness measures chosen by the programmer while preserving high  
22 accuracy. However, as the type of fairness measure could vary among different predictive tasks,  
23 the code may need to be changed accordingly.

24 There are mainly three types of fairness improvement in-processing methods: fairness  
25 constraints, prejudice remover regularizer, and adversarial debiasing. Among these methods, the  
26 fairness constraints method adds fairness constraints to the loss function of the training process  
27 [22]; the prejudice remover regularizer method applies a fairness regularizer to the loss function  
28 [23]; while the adversarial debiasing method develops a predictor and an adversary at the same  
29 time to weaken the power of predicting the protected attribute from the predictive outputs [24].

1 In-processing fairness improvement methods have been used in regression or classification  
2 problems to ensure similar income prediction performance [22,25,26], loan allocation result  
3 [22,23], or violent recidivism prediction performance [23,24,27,28] for people coming from  
4 different race or gender. Yet, they have never been applied to data-driven building models to  
5 achieve uniform energy predictive accuracy among end users.

6 In building engineering domain, the cost-sensitive algorithm, a kind of in-processing methods  
7 that increases classification accuracy of specified conditions through assigning higher  
8 misclassification cost for these conditions, has been used to increase the predictive accuracy of  
9 user-defined conditions [29] or faulty conditions [30–32]. However, they have not been applied to  
10 solve fairness problems. Further, most of existing studies on cost-sensitive algorithms focus on  
11 classification problems instead of regression problems.

12 The previous review of the literature shows that improving fairness for building energy  
13 prediction models is required to ensure uniform predictive performance under all conditions, which  
14 means making sure that services provided based on the predictive result are non-discriminatory.  
15 Besides, there are many fairness improvement methods. Among them, in-processing methods  
16 show the ability to achieve user-defined fairness. However, fairness-related constraints or penalty  
17 should be set based on the specific problem. To the best of the authors' knowledge, there is no  
18 existing study focusing on quantitatively improving fairness among regression problems in building  
19 engineering domain. This study fills this gap and has the following major contributions:

- 20 • Investigate the possibility of improving fairness to have uniform predictive performance  
21 under different conditions for building energy prediction,
- 22 • Propose four in-processing fairness improvement methods for regression problems to  
23 improve fairness, by setting user-defined constraints or penalties for improving predictive  
24 performance similarity between different conditions, and
- 25 • Implement the proposed methods to develop fairness-aware linear regression models for  
26 building energy prediction. Both predictive accuracy and fairness are evaluated.

27 The outline of this paper is: Section 2 introduces the proposed in-processing techniques and  
28 optimization algorithm used for solving the optimization problem defined by in-processing  
29 methods. A case study that applies these methods to improve the energy predictive fairness while

1 preserving predictive accuracy is designed and introduced in this section. In Section 3, results are  
2 analyzed in terms of accuracy measures and fairness measures. Then, Section 4 discusses the effect  
3 of loss functions and optimization algorithms. Finally, Section 5 summarizes the conclusion.

## 4 **2. Methodology**

### 5 **2.1. In-processing fairness improvement methods**

6 Training a model means learning proper model parameters to minimize a loss function  
7 (denote as *Loss*) that indicates the closeness of predicted values to their corresponding actual  
8 values. For regression models, commonly used *Loss* includes mean square error (MSE, see  
9 Equation 1) and mean absolute error (MAE, see Equation 2). MSE calculates the mean of squared  
10 error losses (also called L2 loss). Square loss is the square of residual difference, which is the  
11 difference between the actual value and the predicted value. MAE is the mean of absolute errors,  
12 which are also known as L1 losses. Absolute error is the distance between the actual value and  
13 predicted value. Generally, MSE loss function converges faster than MAE, because the quadratic  
14 function of MSE makes it easier to find the gradient. However, the MAE loss function shows the  
15 advantage of being more robust to outliers than MSE.

$$16 \quad \text{MSE} = \frac{1}{n} \sum_{i=1:n} (y_i - \hat{y}_i)^2 \quad (1)$$

17 where  $n$  is the number of training data samples,  $y$  is the measured value,  $\hat{y}$  is the predicted value.

$$18 \quad \text{MAE} = \frac{1}{n} \sum_{i=1:n} |y_i - \hat{y}_i| \quad (2)$$

19 However, minimizing MSE or MAE could not make sure that the predictive performance is  
20 similar among different conditions. To solve this problem, this section would present four in-  
21 processing fairness improvement methods that add penalties or constraints to *Loss* in order to  
22 narrow the predictive performance difference between conditions defined by the protected attribute.  
23 To make a simple explanation, the original loss function (such as MSE or MAE) without  
24 considering fairness is denoted by *Loss\_ori*, and the protected attribute is assumed as a binary  
25 attribute. Note that these methods could be extended to problems with multi-class protected  
26 attribute through adding pair-wise constraints/penalties.

### 2.1.1. Mean residual difference penalized (MRDP) regression

The loss function of this method, as shown in Equation 3, comprises a  $Loss\_ori$  that illustrates the overall predictive accuracy and a prejudice remover regularizer that indicates the difference magnitude between the mean residual difference when the protected attribute (denoted by  $S$ ) is Positive and the mean residual difference when  $S = \text{Negative}$ . The difference magnitude is squared to avoid negative values. Besides, users could justify the trade-off between accuracy and fairness, though setting the multiplier  $\lambda$  for the regularizer. The bigger the  $\lambda$ , the more important the fairness.

$$\min Loss\_ori + \lambda \left[ \frac{1}{s_0} \sum_{h=1:s_0, S=negative} (y_h - \hat{y}_h) - \frac{1}{s_1} \sum_{k=1:s_1, S=positive} (y_k - \hat{y}_k) \right]^2 \quad (3)$$

where  $\lambda$  is the multiplier of the prejudice remover regularizer;  $S$  is the protected attribute,  $S \in [\text{Negative}, \text{Positive}]$ ;  $s_0$  is the number of training data with  $S = \text{Negative}$ ,  $s_1$  is the number of training data with  $S = \text{Positive}$ .

The regularizer in Equation 3 could be rewritten as Equation 4. It explains that the regularizer calculates the square difference between the mean actual value difference and mean predicted value difference among conditions with  $S = \text{Negative}$  and  $S = \text{Positive}$ .

$$\left[ \left( \frac{1}{s_0} \sum_{h=1:s_0, S=negative} y_h - \frac{1}{s_1} \sum_{k=1:s_1, S=positive} y_k \right) - \left( \frac{1}{s_0} \sum_{h=1:s_0, S=negative} \hat{y}_h - \frac{1}{s_1} \sum_{k=1:s_1, S=positive} \hat{y}_k \right) \right]^2 \quad (4)$$

### 2.1.2. Mean square error penalized (MSEP) regression

In this method, fairness significance is represented by the absolute difference between the MSE when  $S = \text{Positive}$  and MSE when  $S = \text{Negative}$ , see Equation 5. This method avoids the error cancellation within a condition caused by over-predicting for some samples and under-predicting for other samples in the same condition. Similar to MRDP, the trade-off between accuracy and fairness is justified by  $\lambda$ . Note that when  $\lambda = +\infty$ , the MSEP could be considered as a method of Lagrange multiplier that is aimed at finding the minimum  $Loss\_ori$  subject to the equality constraint that makes the MSE when  $S = \text{Positive}$  to be the same as the MSE when  $S = \text{Negative}$ .

$$\min Loss\_ori + \lambda \left| \frac{1}{s_0} \sum_{h=1:s_0, S=negative} (y_h - \hat{y}_h)^2 - \frac{1}{s_1} \sum_{k=1:s_1, S=positive} (y_k - \hat{y}_k)^2 \right| \quad (5)$$





## 2.2. Optimization algorithm

Considering the increased complexity of the loss function by in-processing methods, derivative-free optimization algorithms that do not use derivatives or finite differences [34] would be better options to train regression model parameters. Notable derivative-free optimization algorithms mainly include Bayesian optimization, adaptive coordinate descent, genetic algorithms (GA), differential evolution (DE), simulated annealing, particle swarm optimization (PSO), etc. Among these algorithms, DE has been proofed to be effective in solving constrained optimization problems [35]. Therefore, it will be selected as the solver for optimization problems set by in-processing methods.

DE is a heuristic approach that gets the global optimal solution by iteratively improving the candidate solution based on an evolutionary process [36]. Its general procedure is presented in Figure 1. Detailed description of each step is given as below:

*Population Initialization:* Generate a random or user-defined initial population that contains a set of candidate solutions.

*Fitness assignment:* Evaluate the fitness score of each solution through a fitness function to determine how fit the solution is.

*Selection:* Select a set of solutions (parents) based on some selection procedures for the mutation process to create the unit vector.

*Mutation:* Mutate a unit vector through adding a scaled differential vector to a target vector. Here, the differential vector is the difference between the two or more selected parents, while the target vector is the parent with prioritized direction of creating the unit vector.

*Crossover:* Generate new offspring by crossing over a selected ‘major’ parent (different from the parents used in mutation) and the unit vector created from mutation, and then, add the offspring to the population. Crossover methods mainly include average and intuitive.

*Stop criteria:* Terminate the algorithm if the population has converged (its offspring would not significantly increase the fitness) or if the maximum number of iterations has been reached.

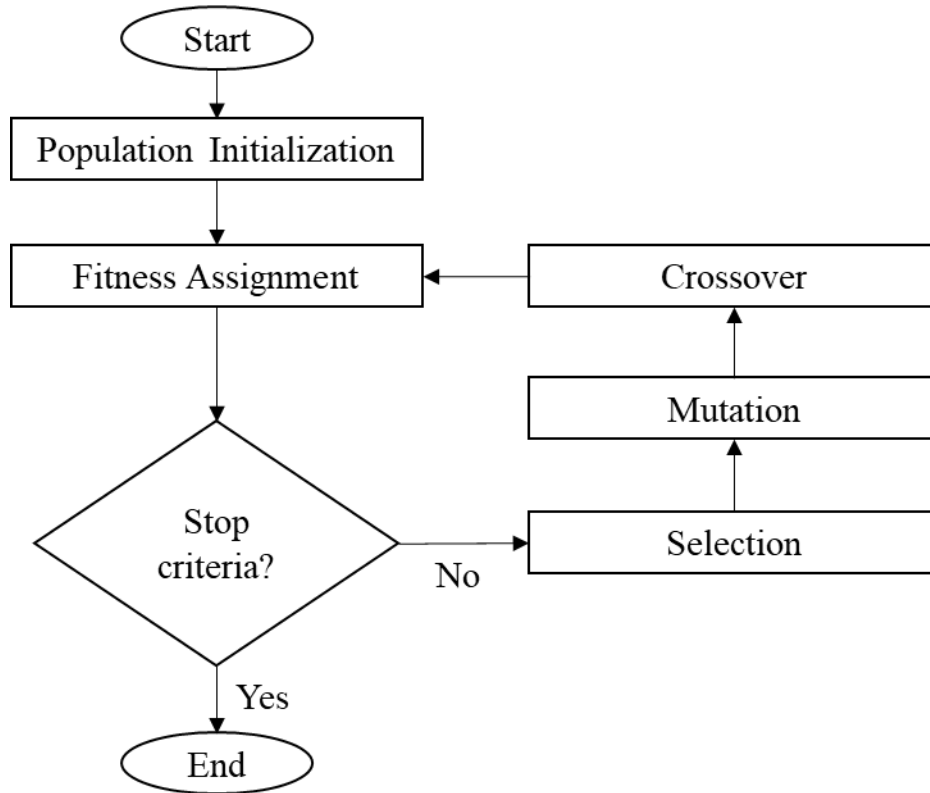


Figure 1: General procedure of a basic DE

### 2.3. Case study: Energy prediction

To investigate the applicability of proposed in-processing methods to solve fairness problems in building engineering domain, a case study is designed to apply these methods to train regressive models to predict hourly energy consumption of an apartment. In the case study, motion status is the binary protected attribute, which means the in-processing methods are aimed at presenting similar energy predictive performance no matter if there is occupancy movement in the apartment. Detailed description of data collection and feature selection are presented in Section 2.3.1, while the study cases are explained in Section 2.3.2.

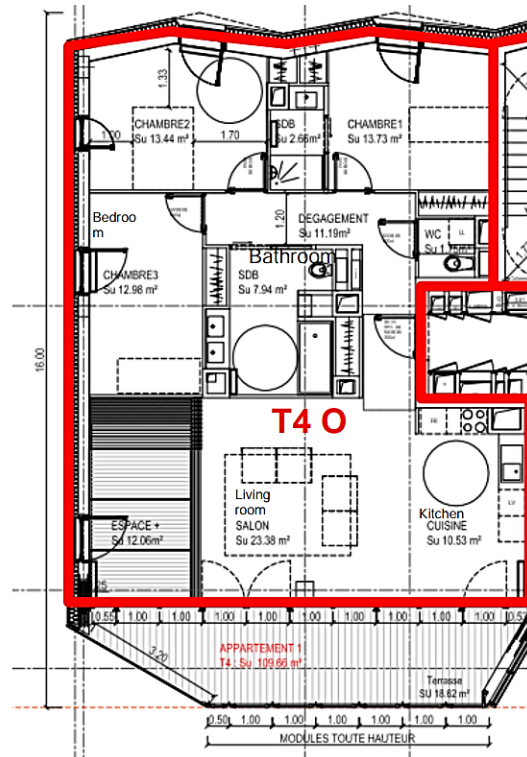
#### 2.3.1. Data description and feature selection

Building-related data used in this study was collected by sensors and HEMS in a three-bedroom apartment in Lyon, France, whose layout is shown in Figure 2. The data collection techniques and devices are explained in details in [37–40]. The original dataset was collected with one-minute time interval during the year of 2016. It contains information of time index (time of the day, day of the week), indoor temperature, indoor humidity, CO<sub>2</sub> concentration, motion status,

1 window opening status, blind position, lighting status and lighting power consumption, as well as  
2 plug power consumption. Note that the summary of plug load and lighting energy consumption  
3 data (Wh) represents the building energy use in this study. Besides, weather information, such as  
4 ambient air temperature, and humidity, wind speed and direction, solar radiation, solar illuminance,  
5 etc., were collected with one-minute time interval from a local weather station in Vaulx-en-Velin,  
6 France.

7 As a larger time interval could increase the data representativity and acceptable predictive  
8 runtime [41], collected data was processed to one-hour resolution. Motion status was recorded as  
9 '1' if there was any movement detected by the corresponding presence sensor during the 60  
10 minutes in that hour. One attribute called 'Motion status\_Total' was added as a candidate input  
11 feature to represent if there is any movement detected in the studied apartment during one hour. It  
12 is assumed as the protected attribute, which means S=Positive is the condition that there is  
13 occupancy movement and S=Negative represents there is no detected movement in the apartment.  
14 Besides, the same sample strategy was applied to lighting status to evaluate if there was any light  
15 opening during one hour. Energy consumption data within one hour was averaged by minute data  
16 and normalized to be the range between 0 and 1. For other attributes, the hourly value was sampled  
17 every 60 minutes. Besides, as energy consumption may belong to time series data that historical  
18 energy consumption would affect future values [11], previous 24 hours' normalized hourly energy  
19 consumption (NHEC) data and previous 168th NHEC are also added as candidate features. Overall,  
20 there are 106 candidate features. A list of these features are presented in the supplementary  
21 information.

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Figure 2: Footprint of the studied apartment

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The NHEC of lighting and plug-ins is the output of data-driven models. Its distribution is shown in Figure 3. In the collected dataset, NHEC is lower than 0.7 most of the time. To select the most representative features for NHEC prediction, correlation between the candidate features and the output is calculated by Equation 8. Features whose correlation with the output is higher than 0.3 are selected as inputs. The selected 15 input features and their correlation with the output is present in Table 1.

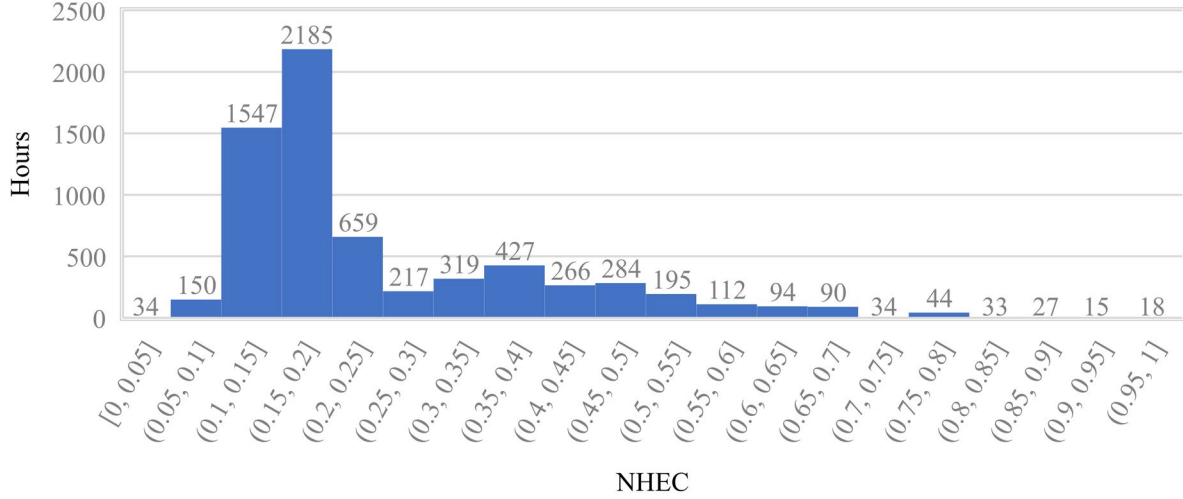


Figure 3: NHEC distribution

$$r_{xy} = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}} \quad (8)$$

where  $r_{xy}$  is the Pearson correlation coefficient,  $x$  is the candidate input feature,  $\bar{x}$  is the mean of corresponding  $x$ ,  $\bar{y}$  is the mean of  $y$ .

Table 1: Selected input features and their correlation with the output attribute

Input feature	Correlation with the output	Input feature	Correlation with the output	Input feature	Correlation with the output
Sun altitude	0.30	Motion status 5	0.42	Motion status Total	0.45
Motion status 1	0.58	Motion status 6	0.53	NHEC t-1	0.57
Motion status 2	0.59	Motion status 7	0.46	NHEC t-2	0.34
Motion status 3	0.57	Motion status 8	0.41	NHEC t-23	0.31
Motion status 4	0.39	Motion status 13	0.32	NHEC t-24	0.33

Note that the number after the name of motion status means the corresponding measurement device, while the time index after NHEC illustrates the normalized hourly energy consumption at the corresponding time, t is the current time.

### 2.3.2. Case description

As the start point of investigating in-processing fairness improvement methods in building energy application, a relatively simple regression model, i.e., linear regression (see Equation 9), is used in this study to predict the normalized hourly energy consumption (NHEC).

$$\hat{y} = w_0 + \sum_{j=1:m} w_j x_j \quad (9)$$

1 where  $w$  and  $w_0$  are parameters that need to be estimated during model training,  $m$  is the number  
 2 of input features.

3 In this study, a reference case that uses MSE as the loss function to learn parameters of the  
 4 developed linear regression model is conducted to be the basis when evaluating the fairness  
 5 improvement ability of in-processing methods. Then, other case studies are designed to investigate  
 6 the effects of in-processing methods and their corresponding  $p$  or  $\lambda$  values on the predictive result,  
 7 see Table 2. MSE is the *Loss\_ori* for these cases.

8 Table 2: Description of study cases

Case name	In-processing methods	$p$ or $\lambda$ value
Reference case		
MRDP 0.6	MRDP	0.6
MRDP 0.8	MRDP	0.8
MSEP 0.6	MSEP	0.6
MSEP 0.8	MSEP	0.8
MRDC 0.6	MRDC	0.6
MRDC 0.8	MRDC	0.8
MSEC 0.6	MSEC	0.6
MSEC 0.8	MSEC	0.8

9 Note that constraints that limit the predicted NHEC within  $[0, 1]$  are added to the loss function of all cases

10 The DE is coded using the scikit-opt package [42], and its hyperparameters are shown in  
 11 Table 3. For all cases, a 10-fold cross validation process is used for training and validating. MAE  
 12 and MSE are used to evaluate the predictive performance. To be more specific, ‘MSE\_TOTAL’  
 13 and ‘MAE\_TOTAL’ is the overall accuracy. ‘1-MSE’ and ‘1-MAE’ means MSE and MAE when  
 14 S=Positive, respectively. ‘0-MSE’ and ‘0-MAE’ is MSE and MAE when S=Negative,  
 15 respectively. Besides, as the goal of this study is to improve fairness in terms of increasing the  
 16 similarity of predictive performance between different conditions, fairness could be evaluated by  
 17 the difference between 1-MSE and 0-MSE or the difference between 1-MAE and 0-MAE. The  
 18 smaller the difference, the better the predictive fairness. On the other hand, it could also be  
 19 evaluated by MSE rate (the rate between 1-MSE and 0-MSE) or MAE rate (the rate between 1-  
 20 MAE and 0-MAE). Higher MSE rate or MAE rate means a better fairness achievement. For  
 21 example, if MSE rate or MAE rate is higher than 0.8, the “80 percent rule” is achieved.

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Table 3: Hyperparameters of DE

Hyperparameter	Meaning	Value
size_pop	Size of population	50
max_iter	Max iteration	1000
prob_mut	Probability of mutation	0.001
F	Coefficient of mutation	0.5

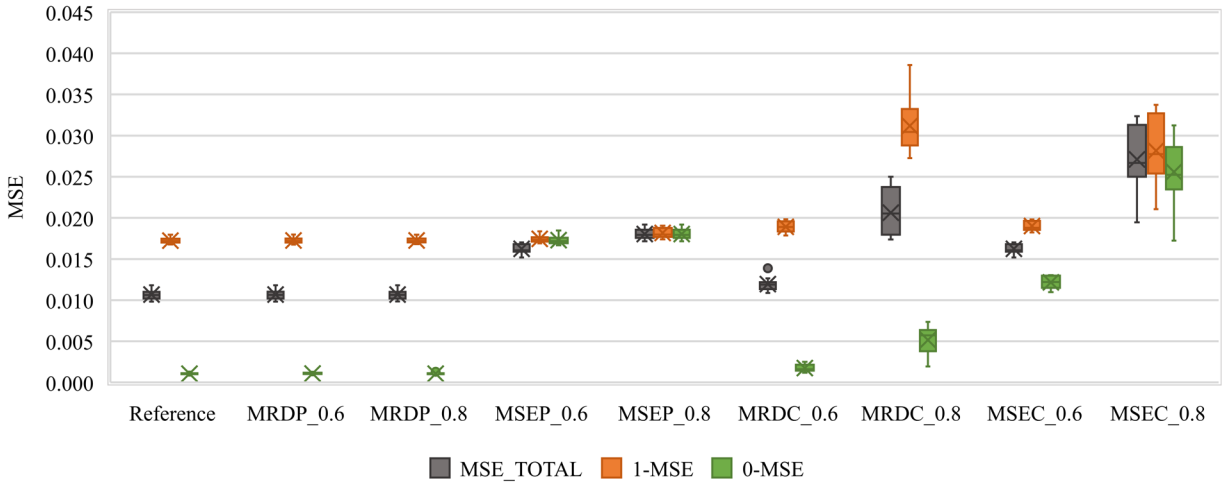
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3 Simulations are run by Python 3.7 on a desktop with Intel Core i7-4790 CPU @3.60GHz  
4 and 8GB of RAM.

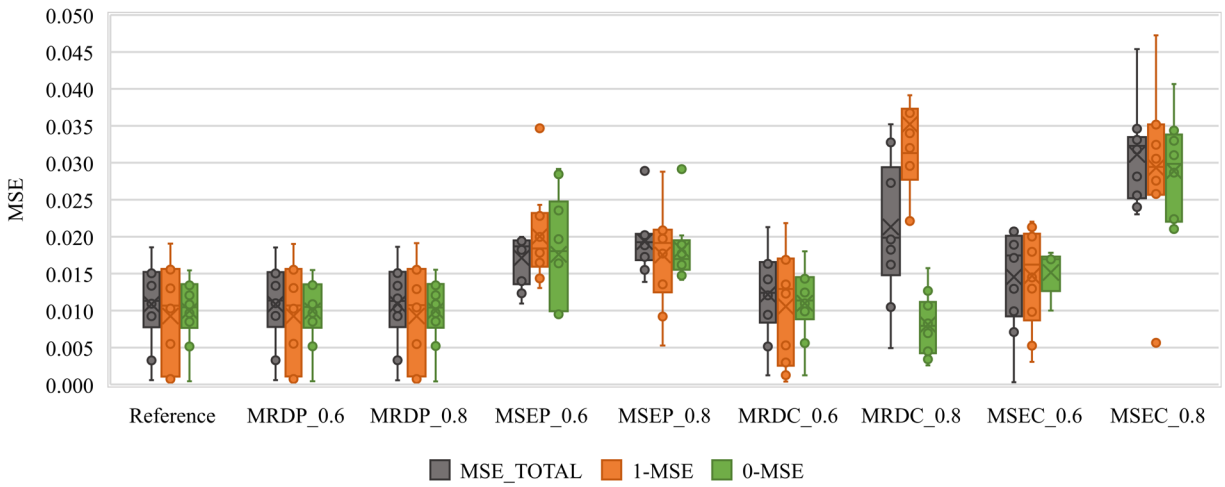
### 5 3. Results

#### 6 3.1. Accuracy in terms of MSE and fairness in terms of MSE rate

7 The effect of four proposed in-processing methods on the predictive MSE during model  
8 training and validation are compared in Figure 4. It shows that MRDP would not affect the  
9 predictive accuracy in terms of MSE no matter during model training or model validation. As  
10 illustrated in Section 2.1.1, the regularizer added by MRDP tries to make the predictive result fair  
11 for conditions with S=Positive and S=Negative to have similar mean residual difference. In other  
12 words, it means to make the difference of mean measured value between the condition that S =  
13 Negative and the condition that S = Positive to be the same as the difference of mean predicted  
14 value between the condition when S = Negative and the condition when S = Positive. As shown in  
15 Figure 5, even in the reference case, the mean predicted NHEC is the same as the mean measured  
16 NHEC, irrelevance of S= Positive or S= Negative. Thus, the regularizer added by MRDP did not  
17 work and it is always almost equal to zero in this case study. Another interesting finding from  
18 Figure 5 is that the energy consumption when there are occupant activities in the apartment (when  
19 S= Positive) is more than twice of the energy consumed during the period that no occupancy  
20 movement is detected (S= Negative). It shows that occupancy-related data would be an important  
21 input for energy prediction of residential buildings.



(a) Model training



(b) Model validation

Figure 4: Effect of in-processing methods on the predictive accuracy in terms of MSE during (a) model training and (b) model validation

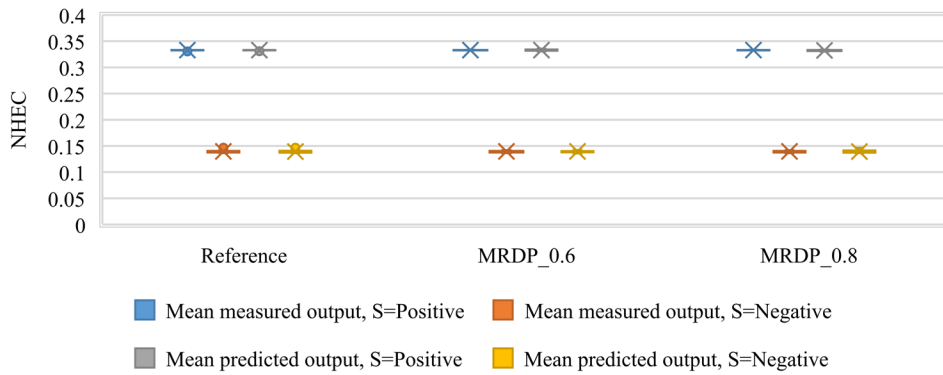
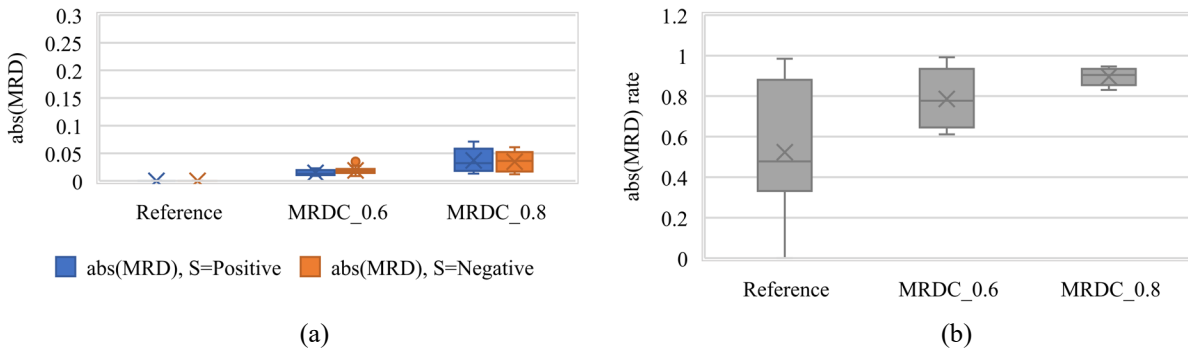


Figure 5: Mean measured NHEC and mean predicted NHEC for conditions S=Positive and S=Negative during model training



1 Besides, from Figure 4(a), during model training, MSEP with  $\lambda=0.6$  could effectively make  
 2 the 1-MSE to be similar to the 0-MSE. However, the predictive accuracy would be decreased as  
 3 the overall MSE is increased from 0.01 to 0.016. Increasing  $\lambda$  from 0.6 to 0.8 would not  
 4 significantly contribute to the similarity of between 1-MSE and 0-MSE. However, the overall  
 5 predictive accuracy of MSEP with  $\lambda=0.8$  is slightly worse than MSEP with  $\lambda=0.6$ . Furthermore,  
 6 Figure 4(b) shows that the effect of MSEP on increasing the similarity between 1-MSE and 0-  
 7 MSE could not be generalized to validation data.

8 Figure 4 also shows that MRDC with  $p=0.6$  shows a slight effect on MSE, while MRDC with  
 9  $p=0.8$  would significantly increase MSE\_TOTAL, 1-MSE and 0-MSE. However, MRDC could  
 10 not narrow the difference between 1-MSE and 0-MSE. This is because MRDC is aimed at making  
 11 the abs(MRD) to be similar enough between S=Positive and S=Negative, instead of increasing the  
 12 similarity in terms of MSE. Increasing  $p$  value for MRDC could effectively increase the fairness  
 13 in terms of abs(MRD) rate during model training (see Figure 6(b)), however, the predictive  
 14 accuracy would be decreased as the abs(MRD) would be increased (see Figure 6(a)). Even if  
 15 increasing  $p$  value could increase the abs(MRD) rate, this pattern is not generalizable during model  
 16 validation (see Figure 7). This problem may be caused by nonconvergence of the optimization  
 17 algorithm when  $p=0.8$ . It could be solved by increasing the maximum iteration number of DE.



18 (a)  
 19 (b)  
 20 Figure 6: Effect of MRDC on the (a) abs(MRD) and (b) abs(MRD) rate during model training  
 21

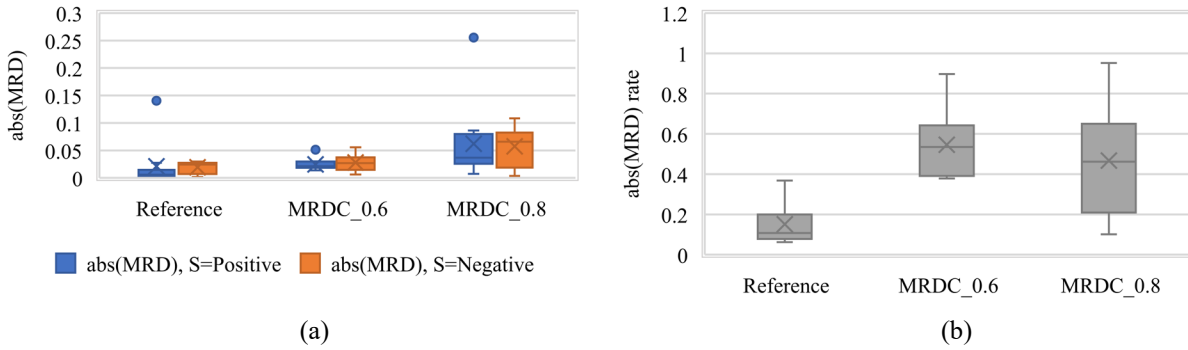


Figure 7: Effect of MRDC on the (a) abs(MRD) and (b) abs(MRD) rate during model validation

Moreover, increasing  $p$  value of MSEC would increase the MSE (see Figure 4), however, the difference between 1-MSE and 0-MSE would be decreased. Figure 8 shows the effect of MSEC on the *Type II* fairness improvement: MSEC with  $p=0.6$  could increase the MSE rate to be higher than 0.6 no matter during model training or model validation, while MSEC with  $p=0.8$  could ensure the MSE rate to be higher than 0.8.

To improve *Type II* fairness in terms of having a high MSE rate, MSEP and MSEC would be suitable solutions. However, from Figure 8, MSEC shows better generalizability on the validation dataset. As Figure 8 shows MRDP does not affect the MSE rate. Although MRDC\_0.6 shows a small MSE rate improvement ability during model training and validation, MRDC\_0.8 significantly decreases the MSE rate from 0.61 to 0.27 during model validation.

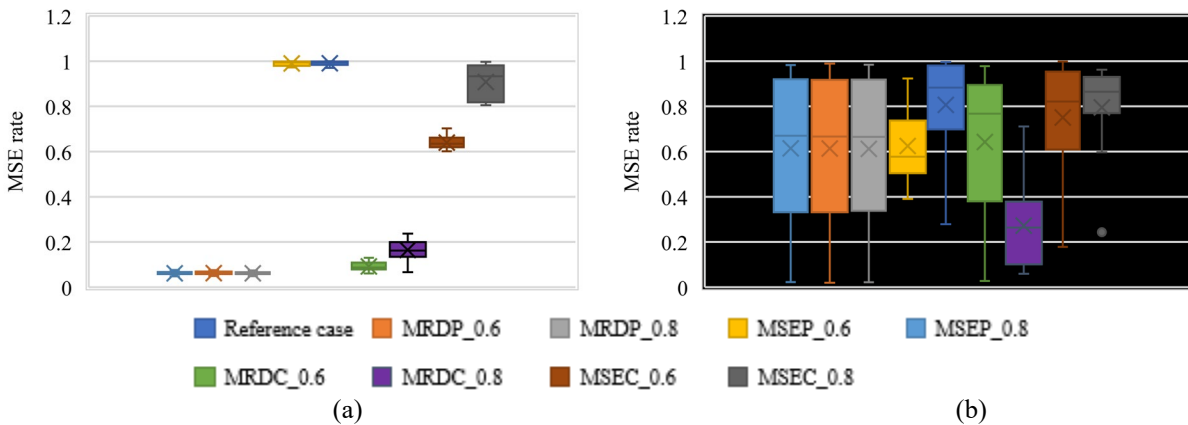
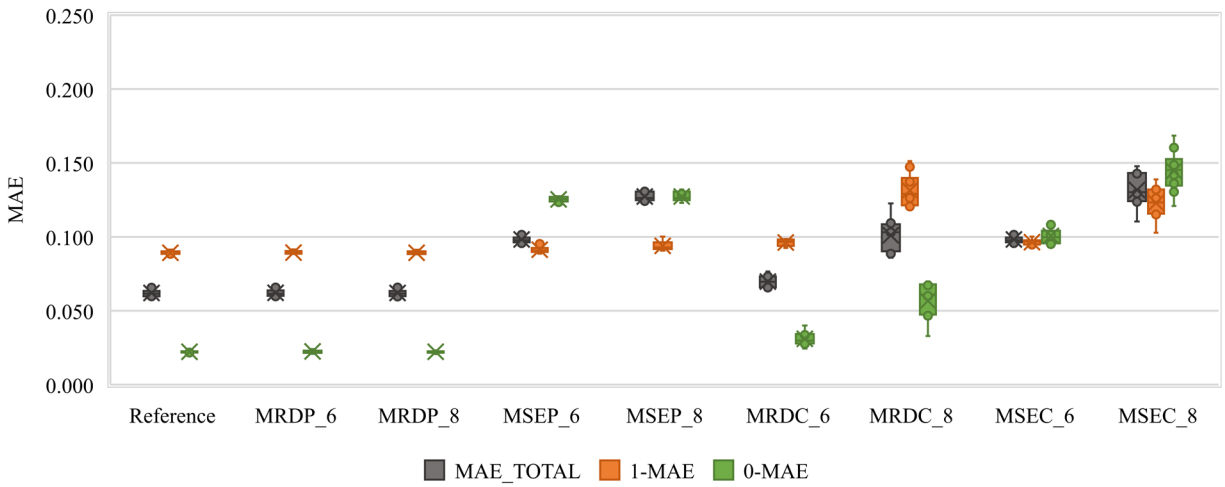


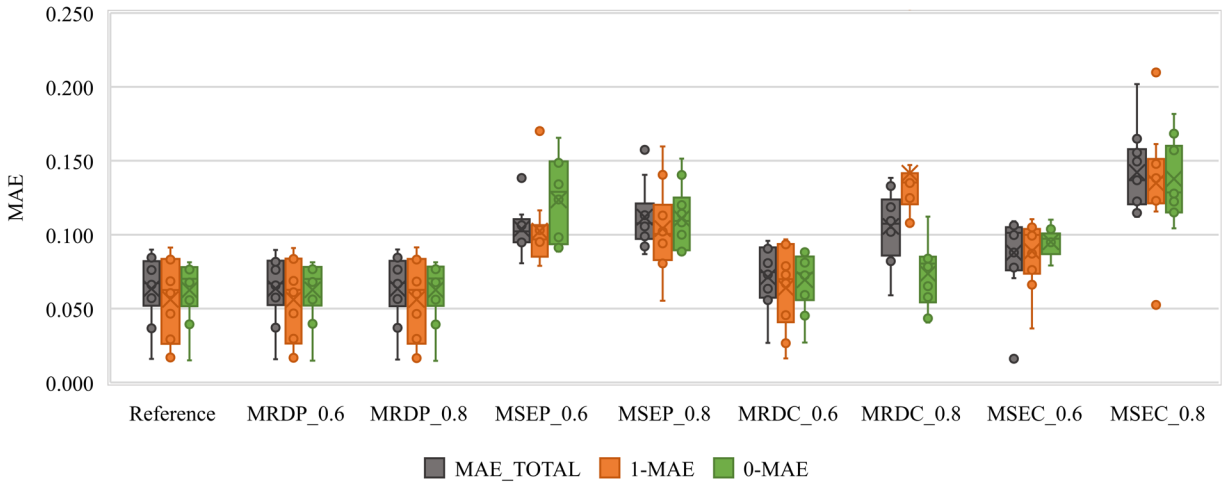
Figure 8: Effect of in-processing methods on the predictive fairness in terms of MSE rate during (a) model training and (b) model validation

1      **3.2. Accuracy in terms of MAE and fairness in terms of MAE rate**

2      As illustrated in Section 3.1, the regularizer added by MRDP is always almost equal to zero  
 3 in this case study. Therefore, MRDP also does not present any effect on the MAE, as shown in  
 4 Figure 9. Besides, MSEP with  $\lambda=0.6$  could effectively decrease the difference between 1-MAE  
 5 and 0-MAE during model training. Increasing  $\lambda$  from 0.6 to 0.8 would not further decrease the  
 6 difference during model training, but the difference would be decreased during validation.  
 7 Furthermore, increasing  $\lambda$  for MSEP would decrease the predictive accuracy because the overall  
 8 MAE is increased.



(a) Model training

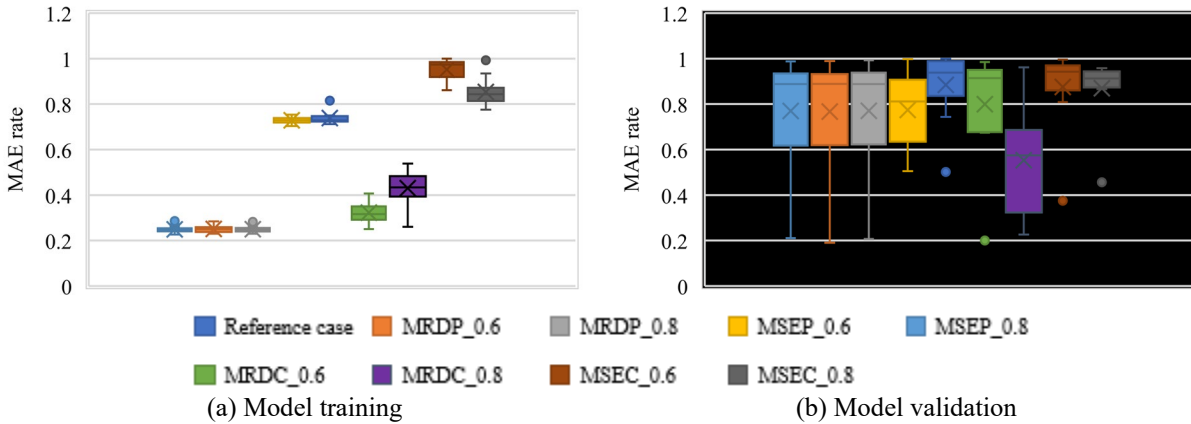


(b) Model validation

Figure 9: Effect of in-processing methods on the predictive accuracy in terms of MAE during (a) model training and (b) model validation

1 From Figure 9, MRDC could not decrease the difference between 1-MSE and 0-MSE,  
 2 although the overall accuracy is decreased. However, MSEC with  $p=0.6$  would effectively  
 3 decrease the difference between 1-MAE and 0-MAE from  $\sim 0.067$  to  $\sim 0.004$  during model training.  
 4 Increasing the  $p$  value would not contribute more to improving the similarity between 1-MAE and  
 5 0-MAE, but would show further harm to the overall predictive accuracy in terms of MAE.

6 The fairness improvement ability in terms of MAE rate is compared between these in-  
 7 processing methods and is presented in Figure 10. Even if the reference case shows a MAE rate  
 8 lower than 0.25 during model training, its MAE rate could reach 0.77 during model validation.  
 9 MRDP does not affect the MAE rate during model training, while other in-processing methods  
 10 would increase the MAE rate. Among them, MRDC with  $p=0.6$  could slightly increase the average  
 11 MAE rate during model training to 0.32, while MRDC with  $p=0.8$  could increase this value to  
 12 0.43. However, even if MRDC\_0.6 shows a slight increase on the MAE rate during model  
 13 validation, MRDC\_0.8 would significantly decrease it. MSEP could increase the MAE rate to be  
 14  $\sim 0.73$  during model training, no matter  $\lambda=0.6$  or  $\lambda=0.8$ . However, a higher  $\lambda$  value shows better  
 15 MAE rate during validation. MSEC shows the best effect on increasing MAE rate, however, it  
 16 shows the different pattern with MSE rate: increasing  $p$  value from 0.6 to 0.8 would not further  
 17 improve the MAE rate.



18  
 19  
 20  
 21  
 22 Figure 10: Effect of in-processing methods on the predictive fairness in terms of MAE rate during (a) model training  
 23 and (b) model validation

## 1 4. Discussion

### 2 4.1. Effect of *Loss\_ori* selection

3 In this study MSE was selected as *Loss\_ori* for in-processing methods, when MAE was  
4 another candidate. The reasons behind this selection include 1) MSE would be more efficient in  
5 term of computation time because the quadratic function of MSE makes it easier to find the  
6 gradient or the direction in which the value of loss function decreases. This reason is proofed  
7 through comparing the training time between using MSE and MAE as the loss function: the  
8 average runtime for using MSE is ~3,400s, while using MAE makes the runtime increase to  
9 ~3,600s; 2) MSE might be more powerful in predicting NHEC values that do not occur frequently  
10 in the training dataset. As illustrated in Section 2.1, MSE is more sensitive to outliers but MAE is  
11 more robust to outliers. It is because the square part of MSE makes it bigger than MAE when  
12 predicting an outlier as the same value. In other words, MSE tries harder to correctly predict  
13 unusual values. In the collected dataset, NHEC is lower than 0.7 most of the time (as shown in  
14 Figure 3), and high NHEC may be treated as outliers during model training, although it is not the  
15 case. Therefore, MSE is selected as *Loss\_ori* to ensure the predictive accuracy for high NHEC  
16 values that are not common in the dataset and suffers a risk of considering as outliers by the data-  
17 driven model.

18 Nonetheless, when comparing the predicted NHEC and measured NHEC for linear regression  
19 models using MSE or MAE as the loss function in Figure 11, it is hard to conclude the better loss  
20 function. Both of them are likely to under-predict the NHEC when the corresponding ground truth  
21 value is higher than 0.7. More effective loss function that gives more weights to the unusual  
22 scenarios is still required to predict high NHEC. Further predictive performance comparison  
23 between MSE and MAE loss functions could be found in Table 4. It shows that using MSE as the  
24 loss function has higher predictive accuracy in terms of MSE, while selecting MAE as the loss  
25 function could ensure a lower predictive error in terms of MAE.

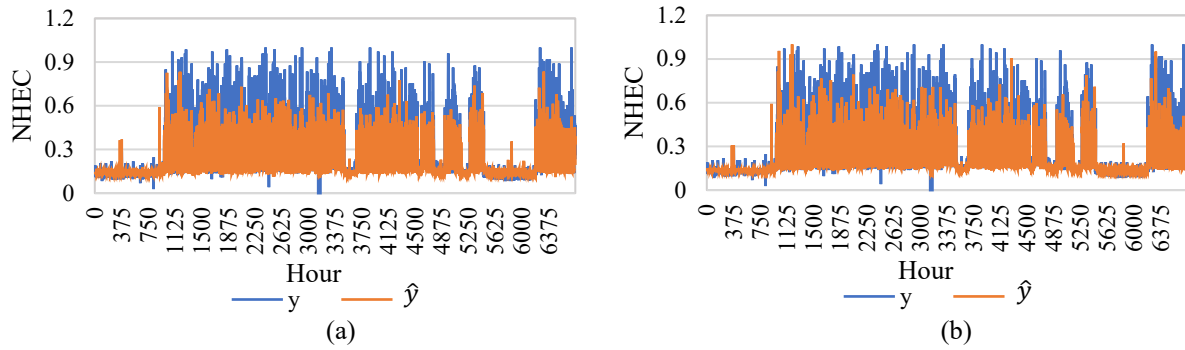


Figure 11: Comparison between  $y$  and  $\hat{y}$  when using (1) MSE or (2) MAE as the loss function

Table 4: Predictive accuracy when using MSE or MAE as the loss function

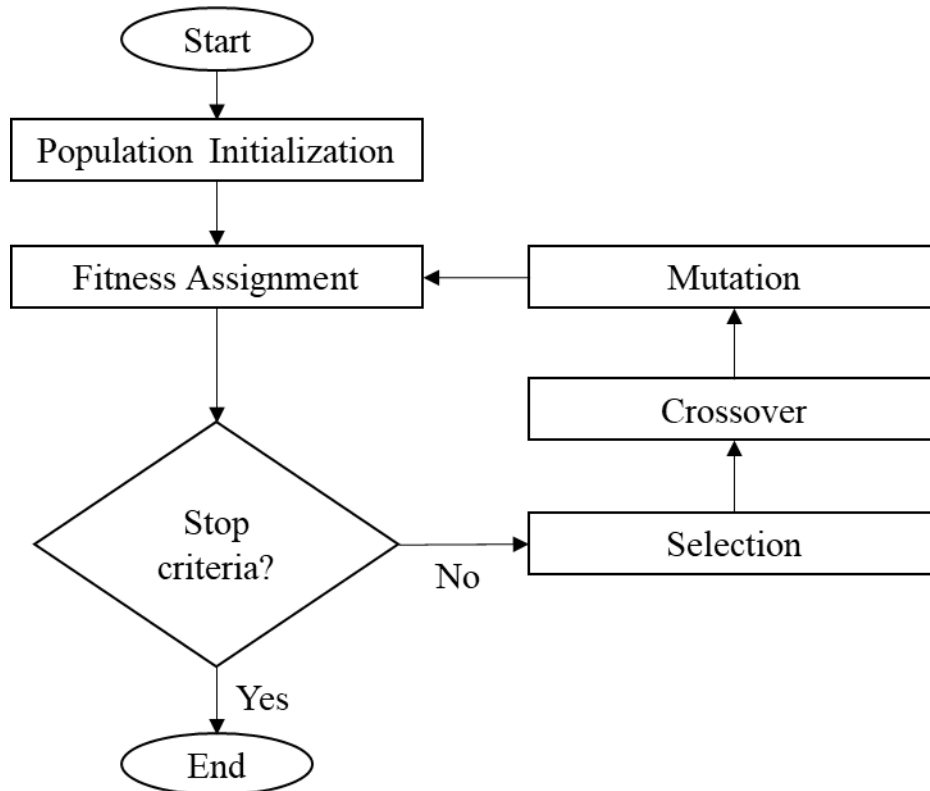
		Performance criteria	
		MSE	MAE
Loss function	MSE	0.0109	0.0634
	MAE	0.0114	0.0605

#### 4.2. Effect of optimization algorithms

Although DE is powerful in solving loss functions of the proposed in-processing algorithms, there are other optimization algorithms that may work well on these constrained optimization problems. For example, genetic algorithm (GA) is a commonly used derivative-free optimization algorithms in building engineering domain. It has been used to do optimal design [43], optimal control [44,45], and predictive model training [46,47], etc.. Therefore, in this section, the runtime and predictive accuracy of reference cases with MSE as the loss function would be compared between DE and GA.

GA is a metaheuristic inspired by the process of natural selection that selects the fittest individual to produce the next generation [48]. It could solve both constrained and unconstrained optimization problems, even if their objective function is discontinuous, nondifferentiable, stochastic, or nonlinear [49]. The general procedure of a basic GA is presented in Figure 12. Note that unlike DE, crossover is processed before mutation in GA. Besides, in the selection step, GA selects two fittest solutions based on their fitness scores, while DE selects a set of parents. Further, GA mutates new offspring based on a probability distribution to maintain the diversity within the

1 population, while the mutation in DE is processed to create a unit vector based on the differential  
 2 vector and target vector.



3  
 4 Figure 12: General procedure of a basic GA

5 In this section, DE and GA have the same population size and maximum iteration time. Their  
 6 predictive accuracy for the reference case is compared in Table 5. It shows that DE always show  
 7 a better accuracy than GA no matter in terms of MSE or MAE. However, GA is much faster than  
 8 DE, as training time of each fold in GA is ~1,700s while DE needs ~3,400s. Therefore, GA would  
 9 be recommended to solve the optimization problem during model training if the runtime is an  
 10 important factor.

11 Table 5: Predictive accuracy comparison between DE and GA

		Model training		Model validation	
		MSE	MAE	MSE	MAE
Optimization algorithm	DE	0.0107	0.0620	0.0109	0.0634
	GA	0.0109	0.0639	0.0112	0.0647

12

## 1 5. Conclusion

2 To improve predictive fairness of regression DDBMs to have uniform predictive accuracy  
3 between different conditions, this study proposed four in-processing methods—MRDP, MSEP,  
4 MRDC, MSEC—to achieve the user-defined trade-off between predictive fairness and overall  
5 accuracy. The fundamental of these methods is to set fairness-related penalties or constraints in  
6 the objective function of model training.

7 A case study was done to apply these in-processing methods to develop linear regression  
8 models for the energy prediction of an apartment. The effect of  $p/\lambda$  values of these methods on the  
9 predictive accuracy and fairness were investigated. Conclusions draw from this case study include:

- 10 • MRDP would not affect the predictive result, because the mean predicted values are almost  
11 equal to the mean measured values under the same condition (S=Positive or S=Negative).
- 12 • MSEP with  $\lambda=0.6$  could significantly decrease the accuracy difference between the  
13 situation that S= Positive and the situation with S=Negative. Increasing  $\lambda$  from 0.6 to 0.8  
14 for MSEP would not narrow the accuracy difference too much, but it would decrease the  
15 overall accuracy.
- 16 • MRDC does not present the ability to decrease the accuracy (MAE or MSE) difference  
17 between different conditions defined by the protected attribute. However, it works good on  
18 increasing the similarity of  $\text{abs}(\text{MRD})$  between S=Positive and S=Negative.
- 19 • MSEC could decrease the difference between 1-MSE and 0-MSE. However, MSEC with  
20  $p=0.6$  results in competitive 1-MAE and 0-MAE similarity compared to MSEC with  $p=0.8$ .  
21 The overall predictive accuracy in terms of MSE and MAE would be decreased when  
22 increase the  $p$  value.
- 23 • MSEC is the most powerful in-processing methods to improve *Type II* fairness in terms of  
24 MSE rate and MAE rate. Besides, MSEP is another good option. It shows better  
25 performance on preserving the overall predictive accuracy than MSEC. However, MRDC  
26 with a high  $p$  value could even destroy the fairness.

27 As the proposed methods show different effects on the accuracy and fairness, researchers are  
28 recommended to select proper methods based on their research objectives. For example, if  
29 improving the MSE rate is the main concern, MSEC would be the best option; if the main objective  
30 is to improve fairness to have a high  $\text{abs}(\text{MRD})$  rate, MRDC could be selected. Furthermore, this



1 study shows some drawbacks: 1) Linear regression models are relatively simple compared with  
2 other regression models, such as deep learning. The simple structure of linear regression makes it  
3 hard to provide high predictive accuracy. Therefore, in the future, integrating the proposed in-  
4 processing methods into more complex and powerful data-driven models would be an interesting  
5 topic. 2) Finding fast and effective optimization algorithms to solve complex objective functions  
6 caused by integrating in-processing methods would be a potential research direction, as the shorted  
7 runtime would make the fairness-aware regression models applicable to develop model predictive  
8 controllers.

9  
10

### 11 **Acknowledgments**

12 The authors would like to express their gratitude to Concordia University for the support through the  
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### 14 **Abbreviations**

abs(MRD)	Absolute Mean Residual Difference
AHUs	Air Handling Units
CV(RMSE)	Coefficient of Variation of the Root Mean Square Error
DDBMs	Data-Driven Buildings Models
DE	Differential Evolution
DT	Decision Tree
FDD	Fault Detection and Diagnosis
GA	Genetic Algorithm
GAN	Generative Adversarial Network
HVAC	Heating Ventilation and Air-Conditioning
HEMS	Home Energy Management System
kNN	k-Nearest-Neighbor
MAE	Mean Absolute Error
MAPE	Mean Absolute Percentage Error
MLP	Multi-Layer Perceptron
MRDC	Mean Residual Difference Constrained Regression

MRDP	Mean Residual Difference Penalized Regression
MSE	Mean Square Error
MSEC	Mean Square Error Constrained Regression
MSEP	Mean Square Error Penalized Regression
NHEC	Normalized Hourly Energy Consumption
PSO	Particle Swarm Optimization
$R^2$	R Square
RF	Random Forest
RMSE	Root Mean Square Error
SMOTE	Synthetic Minority Oversampling Technique
SVM	Support Vector Machine

1

## 2 Nomenclature

$Loss$	Loss function
$Loss_{ori}$	The original loss function without considering fairness
$p$	Weights in MRDC and MSEC. It infers the similarity of predictive performance among different conditions defined by the protected attribute
$r_{xy}$	Pearson correlation coefficient between input feature $x$ and target output $y$
$S$	Protected attribute
$s0$	The number of training data with $S = \text{Negative}$
$s1$	The number of training data with $S = \text{Positive}$
$w_0$	Bias term
$w$	Weight matrix
$x$	Input feature
$\bar{x}$	Mean value of input feature
$y$	Measured value
$\bar{y}$	Mean value of measured value
$\hat{y}$	Predicted value
$\lambda$	Multiplier of the prejudice remover regularizer (MRDP and MSEP)

3

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1 **Supplementary Information:**

2

Table S1: Candidate input features

Input feature	Input feature	Input feature	Input feature	Input feature	Input feature
Day of the week	Irradiance shadow band correction factor	Set-point temperature for heater 3	Blind position 1	Slat angle position 8	NHEC t-9
Time of the day	Direct horizontal irradiance	Set-point temperature for heater 4	Blind position 2	Slat angle position 9	NHEC t-10
Sun altitude	Global horizontal UVA irradiance	Set-point temperature for heater 5	Blind position 3	Slat angle position 10	NHEC t-11
Sun azimuth	Global horizontal UVB irradiance	Set-point temperature for heater 6	Blind position 4	Window opening status 1	NHEC t-12
Global horizontal illuminance	CO <sub>2</sub> concentration 1	Motion status 1	Blind position 5	Window opening status 2	NHEC t-13
Diffuse horizontal illuminance	CO <sub>2</sub> concentration 2	Motion status 2	Blind position 6	Window opening status 3	NHEC t-14
Global vertical north illuminance	CO <sub>2</sub> concentration 3	Motion status 3	Blind position 7	Window opening status 4	NHEC t-15
Global vertical east illuminance	CO <sub>2</sub> concentration 4	Motion status 4	Blind position 8	Window opening status 5	NHEC t-16
Global vertical south illuminance	Indoor temperature 1	Motion status 5	Blind position 9	Window opening status 6	NHEC t-17
Global vertical west illuminance	Indoor temperature 2	Motion status 6	Blind position 10	Window opening status 7	NHEC t-18
Global horizontal irradiance	Indoor temperature 3	Motion status 7	Slat angle position 1	NHEC t-1	NHEC t-19
Giffuse horizontal irradiance	Indoor temperature 4	Motion status 8	Slat angle position 2	NHEC t-2	NHEC t-20
Zenith luminance	Indoor relative humidity 1	Motion status 10	Slat angle position 3	NHEC t-3	NHEC t-21
Relative humidity	Indoor relative humidity 2	Motion status 11	Slat angle position 4	NHEC t-4	NHEC t-22
Wind direction	Indoor relative humidity 3	Motion status 12	Slat angle position 5	NHEC t-5	NHEC t-23
Wind speed	Indoor relative humidity 4	Motion status 13	Slat angle position 6	NHEC t-6	NHEC t-24
Dry bulb temperature	Set-point temperature for heater 1	Motion status 14	Slat angle position 7	NHEC t-7	NHEC t-168
Illuminance shadow band correction factor	Set-point temperature for heater 2	Motion status_Total		NHEC t-8	

1 Note that the number after the name of CO<sub>2</sub> concentration, indoor temperature, indoor relative humidity, set-point  
2 temperature for heaters, motion status, blind position, slat angle position, and window opening status means the  
3 corresponding measurement device, while the time index after NHEC illustrates the normalized hourly energy  
4 consumption at the corresponding time, t is the current time.

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